

Name: _____

Date: _____

Polynomials

Class: Algebra

Topic: Graphing Polynomials

Notes

Polynomial: _____

Linear Function: _____

Parent Function: _____

of Roots: _____

Sketch:

Quadratic Function: _____

Parent Function: _____

of Roots: _____

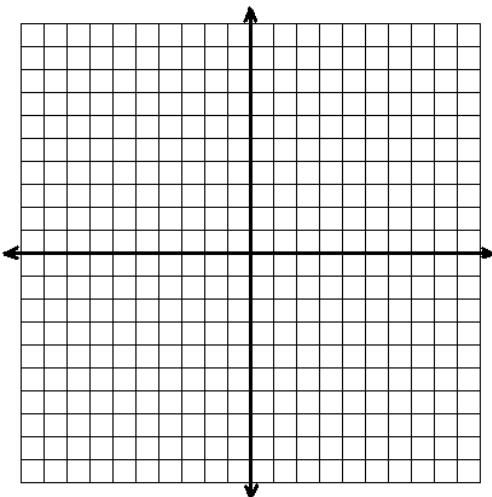
Sketch:

Cubic Function: _____

Parent Function: _____

of Roots: _____

Graph $g(x)=x^3$ and state the roots.



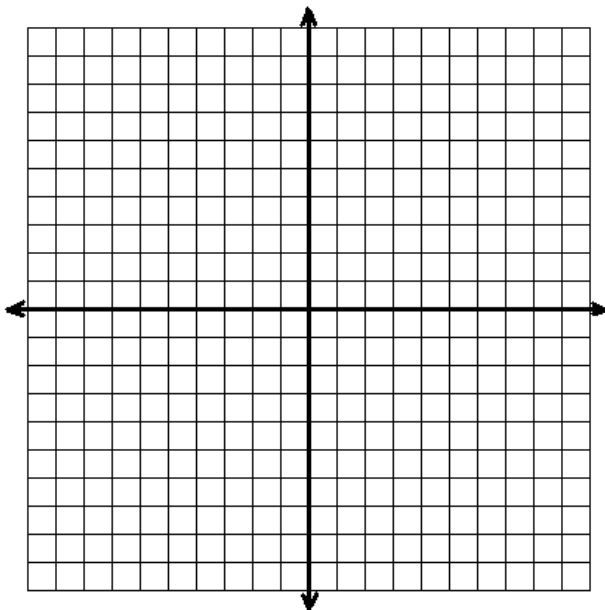
The coefficient of the leading term is **Positive/Negative**?

The exponent of the leading term is **even/odd**?

The end behavior is **down/up and down/up**?

Model #2

Graph $f(x)=x^3 + x$ and state the roots.



Roots: _____

The coefficient of the leading term is **Positive/Negative**?

The exponent of the leading term is **even/odd**?

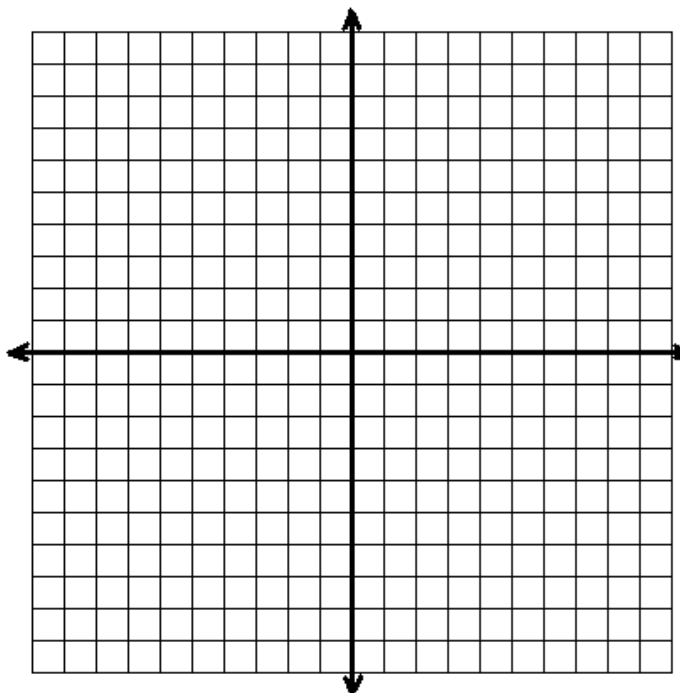
The end behavior is **down/up and down/up**?

CFU_Think-Pair-Share

State the similarities and differences among the graphs $g(x) = x^3$ and $f(x) = x^3 + x$

Model #3

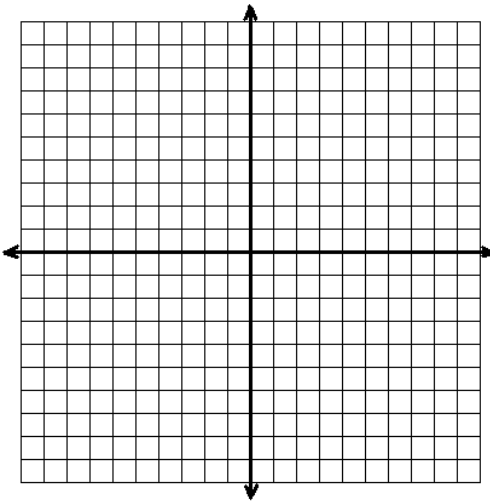
Graph $g(x)=x^3 - x$ and
 $f(x) = x^3 - 4x$



Part B_ Describe the shift that occurred.

CFU Think-Pair-Share

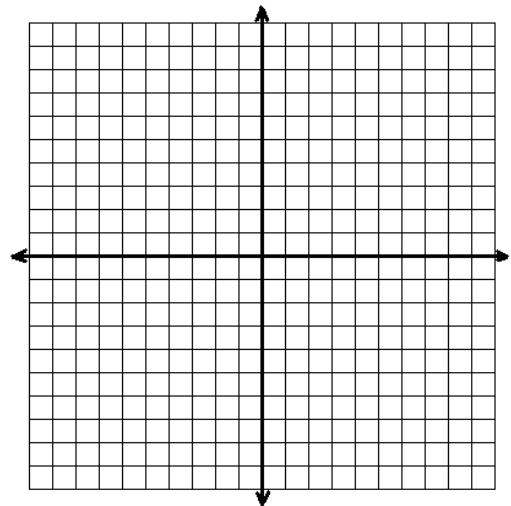
1) Graph $g(x)=x^3$ and $f(x) = 2x^3 - 8x$



Part B_ Describe the shift that occurred.

2) For the graph $f(x) = 2x^3 - 8x$ answer the following questions.

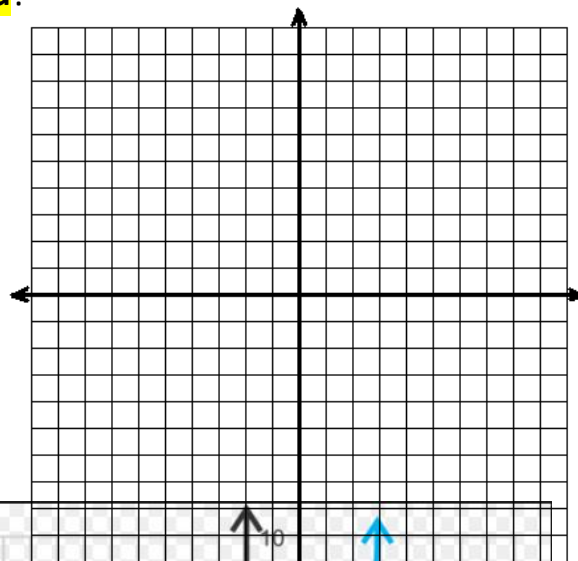
- The coefficient of the leading term is **Positive/Negative**?
- The exponent of the leading term is **even/odd**?
- The end behavior is **down/up** and **down/up**?
- Graph the following polynomial.



3) **Got It?** What is the graph of $y = -x^3 + 2x^2 - x - 2$? Describe the graph.

- a) The coefficient of the leading term is **Positive/Negative**?
- b) The exponent of the leading term is **even/odd**?
- c) The end behavior is **down/up and down/up**?
- d) Graph the following graph

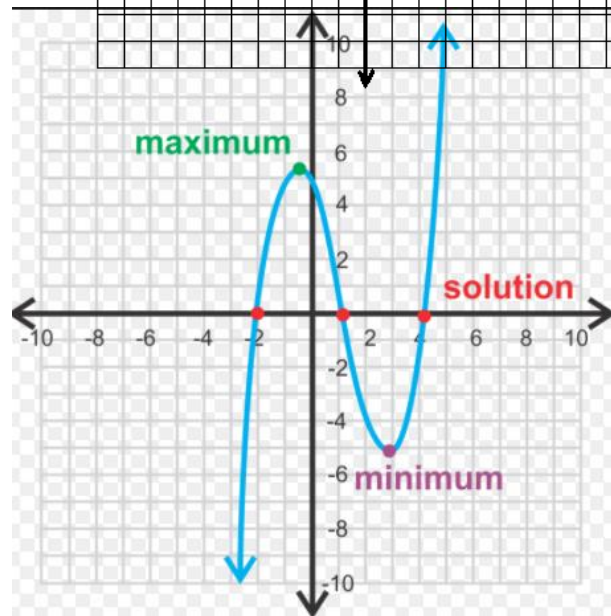
$$y = -x^3 + 2x^2 - x - 2$$



Guided Practice

- 1) Based on the graph below, write an expression that is a possible factorization of $p(x)$

Answer: _____



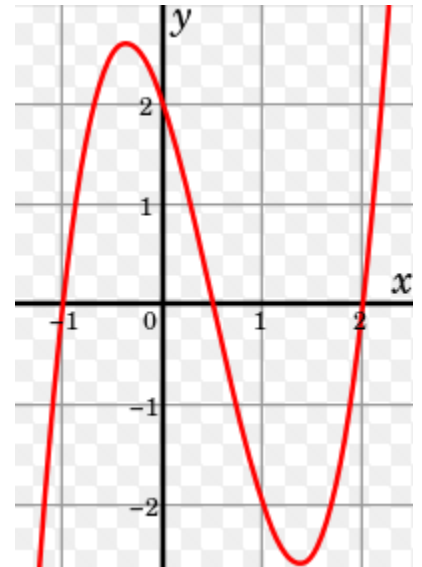
- 2) Based on the graph below, write an expression that is a possible factorization of $p(x)$

Answer: _____



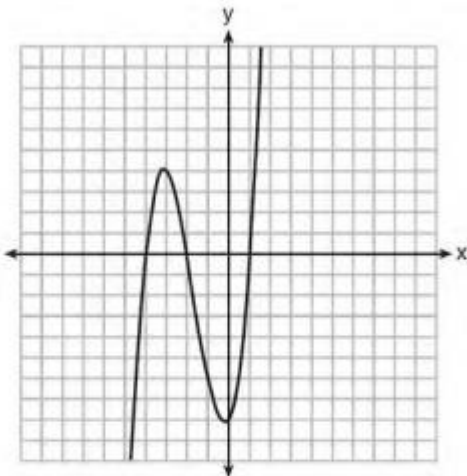
- 3) Based on the graph below, write an expression that is a possible factorization of $p(x)$?

Answer: _____



CFU Think-Pair-Share

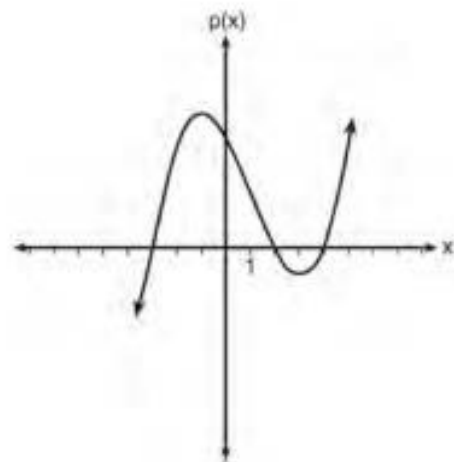
The graph of $f(x)$ is shown below.



Which function could represent the graph of $f(x)$?

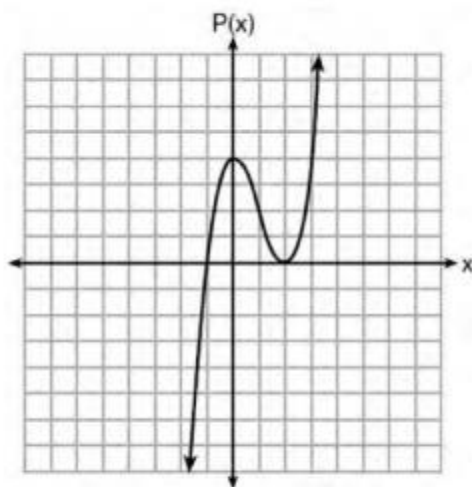
- 1) $f(x) = (x + 2)(x^2 + 3x - 4)$
- 2) $f(x) = (x - 2)(x^2 + 3x - 4)$
- 3) $f(x) = (x + 2)(x^2 + 3x + 4)$
- 4) $f(x) = (x - 2)(x^2 + 3x + 4)$

Based on the graph below, which expression is a possible factorization of $p(x)$?



- 1) $(x + 3)(x - 2)(x - 4)$
- 2) $(x - 3)(x + 2)(x + 4)$
- 3) $(x + 3)(x - 5)(x - 2)(x - 4)$
- 4) $(x - 3)(x + 5)(x + 2)(x + 4)$

Wenona sketched the polynomial $P(x)$ as shown on the axes below.

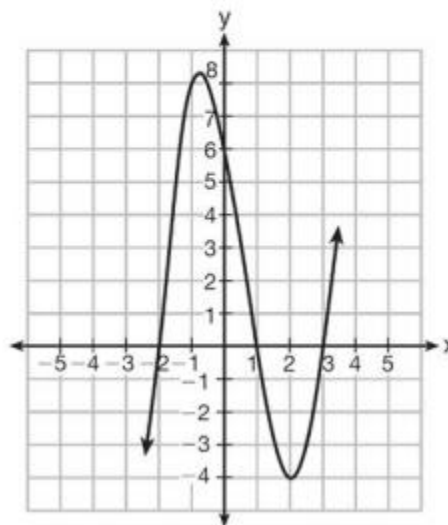


Which equation could represent $P(x)$?

- 1) $P(x) = (x + 1)(x - 2)^2$
- 2) $P(x) = (x - 1)(x + 2)^2$
- 3) $P(x) = (x + 1)(x - 2)$
- 4) $P(x) = (x - 1)(x + 2)$

Which equation(s) represent the graph below?

- I $y = (x + 2)(x^2 - 4x - 12)$
- II $y = (x - 3)(x^2 + x - 2)$
- III $y = (x - 1)(x^2 - 5x - 6)$



The zeros of the function $f(x) = 2x^3 + 12x - 10x^2$ are

- 1) $\{2, 3\}$
- 2) $\{-1, 6\}$
- 3) $\{0, 2, 3\}$
- 4) $\{0, -1, 6\}$

Independent Practice: Use your graphing calculator to answer the following questions.

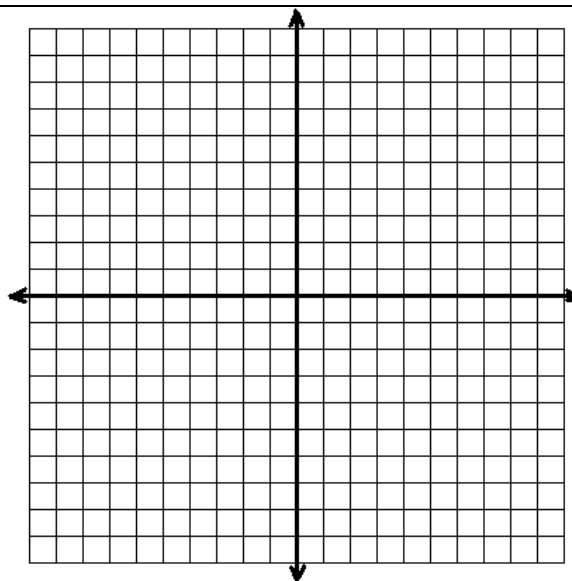
In the functions $f(x) = kx^2$ and $g(x) = |kx|$, k is a positive integer. If k is replaced by $\frac{1}{2}$, which statement about these new functions is true?

- 1) The graphs of both $f(x)$ and $g(x)$ become wider.
- 2) The graph of $f(x)$ becomes narrower and the graph of $g(x)$ shifts left.
- 3) The graphs of both $f(x)$ and $g(x)$ shift vertically.
- 4) The graph of $f(x)$ shifts left and the graph of $g(x)$ becomes wider.

Given the graph of the line represented by the equation $f(x) = -2x + b$, if b is increased by 4 units, the graph of the new line would be shifted 4 units

- 1) right
- 2) up
- 3) left
- 4) down

The vertex of the parabola represented by $f(x) = x^2 - 4x + 3$ has coordinates $(2, -1)$. Find the coordinates of the vertex of the parabola defined by $g(x) = f(x - 2)$. Explain how you arrived at your answer. [The use of the set of axes below is optional.]



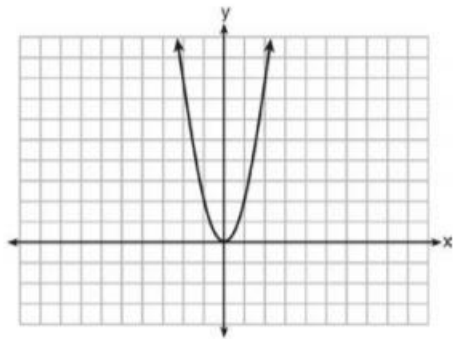
When the function $f(x) = x^2$ is multiplied by the value a , where $a > 1$, the graph of the new function, $g(x) = ax^2$

- 1) opens upward and is wider
- 2) opens upward and is narrower
- 3) opens downward and is wider
- 4) opens downward and is narrower

How does the graph of $f(x) = 3(x - 2)^2 + 1$ compare to the graph of $g(x) = x^2$?

- 1) The graph of $f(x)$ is wider than the graph of $g(x)$, and its vertex is moved to the left 2 units and up 1 unit.
- 2) The graph of $f(x)$ is narrower than the graph of $g(x)$, and its vertex is moved to the right 2 units and up 1 unit.
- 3) The graph of $f(x)$ is narrower than the graph of $g(x)$, and its vertex is moved to the left 2 units and up 1 unit.
- 4) The graph of $f(x)$ is wider than the graph of $g(x)$, and its vertex is moved to the right 2 units and up 1 unit.

The graph of the equation $y = ax^2$ is shown below.



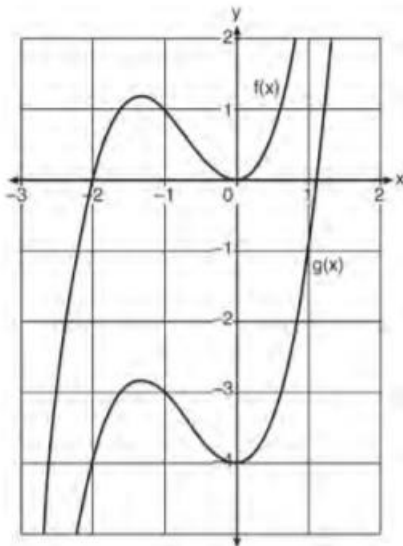
If a is multiplied by $-\frac{1}{2}$, the graph of the new equation is

- 1) wider and opens downward
- 2) wider and opens upward
- 3) narrower and opens downward
- 4) narrower and opens upward

If the original function $f(x) = 2x^2 - 1$ is shifted to the left 3 units to make the function $g(x)$, which expression would represent $g(x)$?

- 1) $2(x - 3)^2 - 1$
- 2) $2(x + 3)^2 - 1$
- 3) $2x^2 + 2$
- 4) $2x^2 - 4$

In the diagram below, $f(x) = x^3 + 2x^2$ is graphed. Also graphed is $g(x)$, the result of a translation of $f(x)$.



Determine an equation of $g(x)$. Explain your reasoning.