Ms. Streffacio
Class: $\qquad$
I can:

## Do Now (3 minutes to complete):

Write out your rules for exponents:

| Product Rule | $y^{a} \times y^{b}$ |
| :--- | :--- |
| Quotient Rule | $\frac{z^{a}}{z^{b}}$ |
| Power to Power Rule | $\left((x)^{a}\right)^{b}$ |
| Zero Product Rule | $\frac{b^{0}}{x^{4}}$ |
| Negative Rule | $x^{3}$ |

## Teacher Model (10 minutes) You Watch, Listen, Copy:

$$
\frac{x^{3} x^{-5}}{x^{4}}
$$

$$
\frac{\left(\left(2 x^{2}\right)\left(y^{3}\right)\right)^{4}}{\left(x^{3} y^{4}\right)^{3}} \quad \frac{y^{12}}{y^{-7}} \cdot \frac{y^{10}}{y^{23}}
$$

## Check for Understanding-Did you understand the Model? (2 minutes) Teacher will check!

Simplify: $\frac{32^{-1}}{32^{6}}$. Write your answer with a positive exponent.

Show your work.

The expression is a quotient of powers.

Solution: $\qquad$

## We Do Together (10 minutes):

Jude incorrectly simplified the expression $\left(\frac{1}{2}\right)^{2} \times \frac{1}{2} \times\left(\frac{1}{2}\right)^{3}$, as shown below.

$$
\left(\frac{1}{2}\right)^{2} \times \frac{1}{2} \times\left(\frac{1}{2}\right)^{3}=\left(\frac{1}{8}\right)^{6}=\frac{1}{262,144}
$$

Describe the mistake that Jude made.

Answer

Correctly simplify the expression.

$$
\left(\frac{1}{2}\right)^{2} \times \frac{1}{2} \times\left(\frac{1}{2}\right)^{3}
$$

Final Check for Understanding before I send you to Independent Practice! Teacher will Check (4 minutes):

Which expression is equivalent to $\left(3^{4} \cdot 5^{4}\right)^{-3}$ ?
A $\frac{1}{15^{5}}$
B $\quad 15^{-48}$
C $\frac{1}{15^{12}}$
D $15^{5}$
Tania chose B as the correct answer. How did she get that answer?
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Independent Practice (on your own):

What value of $n$ makes the following equation true?

$$
\frac{4^{8}}{\left(4^{2}\right)^{-3}} \div 4^{4}=4^{n}
$$

Show your work.

Remember the order of operations. Simplify the expression within the parentheses first.


Josh examines the expression $\frac{5^{-m}}{5^{m}}$, where $m$ is greater than 0 .
He claims that the expression has a value equal to 1 because it simplifies to $5^{\circ}$, and any integer to the 0 power is 1 .

Is Josh correct? Explain why or why not.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Jacob thinks that $3^{5}$ is $5 \cdot 5 \cdot 5$, or 125 . Explain what Jacob is doing wrong.

Margo's dad offers to give her $5 ¢$ on Sunday. Then for each day of the week, he offers to give her 5 times the amount from the previous day. How much will he give her on Saturday? Write an expression to show how much Margo's dad gives her on Saturday.

Is $2^{4}$ equal to $2 \cdot 4$ ? Explain.

> A bacterium cell splits into 2 cells every hour. Write and evaluate an exponential expression to find how many cells there will be in 6 hours. Then use your answer to help you find the number of hours it will take for there to be 1,024 cells.

## Show your work.

Solution: $\qquad$
$\qquad$

The population of California is about 39 million. Is this greater than or less than $10^{7}$ ? Explain.
$\qquad$
$\qquad$

Write each of the numbers $1,8,27,64$, and 125 as a base raised to the third power.
$1=\square^{3}$
$8=\square^{3}$
$27=\square^{3}$
$64=\square^{3}$
$125=$


The exponential expression $2^{8}$ has a value of 256 . Write two other exponential expressions that have a value of 256 . Explain how you got your answers. (Begin by writing out $2^{8}$ as the product of 2 s .)
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Simplify: $\left(7^{5}\right)^{6}$. Write your answer using an exponent.

Simplify: $\left(6^{3}\right)\left(9^{3}\right)$. Write your answer using an exponent.

Is the statement $\left(3^{5}\right)^{4}=\left(3^{4}\right)^{5}$ true? Explain your reasoning.

Simplify: $\left(7^{5}\right)\left(4^{5}\right)$. Write your answer using an exponent.
$\qquad$
Explain in words how to simplify: $\left(153^{2}\right)^{7}$.

Is the statement $\left(10^{5}\right)\left(4^{5}\right)=14^{5}$ true? Explain your reasoning.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

What is the value of $x$ in the equation $\left(5^{x}\right)^{5}=5^{35}$ ? Explain.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Nicholas says that $\left(2^{6}\right)\left(2^{6}\right)$ equals $2^{12}$ and also equals $4^{6}$.
Do you agree? Explain your reasoning.

Use the properties of exponents to write an equivalent expression that is a product of distinct primes, each raised to an integer power.
$\frac{10^{5} \cdot 9^{2}}{6^{4}}=$

Compute: $3^{3} \times 3^{2} \times 3^{1} \times 3^{0} \times 3^{-1} \times 3^{-2}=$
Compute: $5^{2} \times 5^{10} \times 5^{8} \times 5^{0} \times 5^{-10} \times 5^{-8}=$
Compute for a nonzero number, $a$ : $a^{m} \times a^{n} \times a^{l} \times a^{-n} \times a^{-m} \times a^{-l} \times a^{0}=$

For Exercises 5-10, write an equivalent expression, in exponential notation, to the one given, and simplify as much as possible.

## Exercise 5

$5^{-3}=$

## Exercise 7

$3 \cdot 2^{-4}=$

## Exercise 6 <br> $\frac{1}{8^{9}}=$

## Exercise 8

Let $x$ be a nonzero number.

$$
x^{-3}=
$$

## Exercise 10

Let $x, y$ be two nonzero numbers.
$x y^{-4}=$
$9^{15} \cdot \frac{1}{9^{15}}=$
$\left(7(123456.789)^{4}\right)^{0}=$ $2^{2} \cdot \frac{1}{2^{5}} \cdot 2^{5} \cdot \frac{1}{2^{2}}=\frac{2^{2}}{2^{2}} \cdot \frac{2^{5}}{2^{5}}$
$\frac{x^{41}}{y^{15}} \cdot \frac{y^{15}}{x^{41}}=\frac{x^{41} \cdot y^{15}}{y^{15} \cdot x^{41}}$
$\qquad$

## 8.EE. 1

1. Determine if each expression is equivalent to $\frac{7^{6}}{7^{3}}$.

Choose Yes or No for each expression.
a. $\left(7^{9}\right)\left(7^{-6}\right)$No
b. $7^{-8} \div 7^{-11}$ $\square$ YesNo
c. $\left(7^{5}\right)\left(7^{3}\right) \div 7^{4}$YesNo
d. $7^{-3} \times 7^{6}$ Yes No
e. $\left(7^{3}\right)^{0}$
 No
2. Which statement is true about the value of $\left(6^{-n}\right)\left(6^{n}\right)$ ?

A For $n<0$, the value of the expression is greater than 1 .
B For $n>0$, the value of the expression is 0 .
C For all $n$, the value of the expression is less than 1 .
D For all $n$, the value of the expression is 1 .
3. Which expressions are equivalent to $13^{6} \div \frac{\left(13^{9}\right)\left(13^{-4}\right)}{13^{-2}}$ ?

Choose all that apply.
A $\frac{1}{(-13)^{0}}$
B $(-1)^{4}$
C $(-1)^{7}$
D $1^{13}$
E $\frac{1}{13^{-1}}$
4. Look at the equations below. Tell whether each equation is True or False.
a. $3^{5} \cdot 3^{7}=3^{35}$

b. $\left(6^{3} \cdot 3^{3}\right)^{2}=18^{6}$
$\square$ True $\square$ False
c. $7^{-6} \cdot \frac{1}{7^{4}}=\frac{1}{7^{10}}$
$\square$ True
False
d. $4^{4} \cdot 4^{2}=4^{6}$

e. $\frac{13^{-4}}{13^{4}}=13^{0}$ $\square$
$\square$ False
f. $\left(2^{3} \cdot 8^{3}\right)^{0}=16^{9}$ $\square$ True $\square$
5. Tyler simplified the expression $5^{4} \cdot 5^{-9}$. All of his work except his answer is shown below.

$$
\begin{aligned}
5^{4} \cdot 5^{-9} & =5^{4+(-9)} \\
& =5^{-5} \\
& =?
\end{aligned}
$$

Which expression is the correct answer for Tyler's work?
A $5^{5}$
B $\frac{1}{5^{5}}$
C $\frac{1}{5^{-5}}$
D 5
6. A cylinder and a cone have congruent heights and radii. What is the ratio of the volume of the cone to the volume of the cylinder?

A $1: 1$
B $1: 3$
C 1:6
D $1: 9$
7. Which of the equations listed below are linear equations?

Equation I: $C=2 \pi r$

Equation II: $\boldsymbol{A}=\pi r^{2}$
Equation III: $V=\frac{4}{3} \pi r^{3}$
A equation I only
B equation II only
C equations I and III
D equations II and III
8. The scatter plot below shows the points scored and the points allowed by the Bulldogs football team for several games.


Which association (correlation) best describes the data?

A no association (correlation)
B positive association (correlation)
C negative association (correlation)
D nonlinear association (correlation)
9. Simplify.

$$
5^{-8} \times 5^{4}
$$

A $\frac{1}{5^{4}}$
B $\frac{1}{5^{32}}$
C $-5^{2}$
D $-5^{12}$
12. A certain human red blood cell has a diameter of 0.000007 meters. Which expression represents this diameter, in meters, in scientific notation?

A $7 \times 10^{-6}$
B $7 \times 10^{-5}$
C $7 \times 10^{6}$
D $7 \times 10^{5}$
13. What is the value of $n$ in the equation shown below?

$$
2^{2} \times 2^{n}=\left(2^{4}\right)^{3}
$$

A 5
B 6
C 10
D 12
14. Which expression is equivalent to $2^{2} \cdot \frac{2}{2^{4}}$ ?

A $2^{-2}$
B $2^{-1}$
C $2^{6}$
D $2^{7}$
15. What is the value of the expression $\frac{3^{-3} \times 3^{8}}{3^{6}}$ ?
A. $\frac{1}{81}$
B. $\frac{1}{3}$
C. 3
D. 81
16. Which exponential expression is equal to $2^{-5} \cdot 2^{8}$ ?

A $\frac{2^{2}}{2^{-1}}$
B $\left(2^{3}\right)^{-1}$
C $\frac{2^{-2}}{2^{-1}}$
D $\left(2^{-1}\right)^{3}$
$\qquad$

## Do Now (3 minutes to complete):

Write 0.0000003105 in scientific notation. Explain how you found your answer.

## Show your work.

Is the number between 0 and 2 or is it greater than 1 ? What does that tell you about the number in scientific notation?

Solution: $\qquad$

## Teacher Model (10 minutes) You Watch, Listen, Copy:

Earth is about $1.5 \times 10^{4}$ kilometers from the Sun, while the planet Neptune is almost $4.5 \times 10^{9}$ kilometers from the Sun. The distance from Neptune to the Sun is about how many times the distance from Earth to the Sun?

## Check for Understanding- Did you understand the Model? (2 minutes) Teacher will check!

The average masses of several insects or animals are shown in the table. The average mass of a hummingbird is about how many times the average mass of a housefly?

| Insect or Animal | Average Mass (g) |
| :---: | :---: |
| Ant | $4 \times 10^{-3}$ |
| Bee | $1 \times 10^{-1}$ |
| Housefly | $1.2 \times 10^{-2}$ |
| Ruby-throated <br> hummingbird | 3.6 |

## We Do Together (10 minutes):

The population of the United States is about $3.2 \times 10^{8}$. The population of the United States is about 80 times the population of Oregon. Write the population of Oregon in scientific notation.

## Final Check for Understanding before I send you to Independent Practice! Teacher will Check (4 minutes):

The mass of Earth's moon is about $7 \times 10^{22}$ kilograms. The mass of Jupiter is about $1.89 \times 10^{27}$ kilograms. The mass of Jupiter is about how many times the mass of Earth's moon?

Show your work.


Solution: $\qquad$

Independent Practice (In designated groups or on your own):
The area of the Pacific Ocean is about $1.56 \times 10^{8}$ square kilometers. The area of the East China Sea is about $1.2 \times 10^{6}$ square kilometers. Tell whether each statement is True or False.
a. The area of the Pacific Ocean is about $15,600,000$ square kilometers. $\square$ True $\square$ False

b. The area of the Pacific Ocean is about 130 times the area of the East China Sea. $\square$ False
c. The area of the East China Sea is about 130 times the area of the Pacific Ocean. $\square$ False
d. The area of the East China Sea is about $1,200,000$ square kilometers. $\square$ True $\square$ False

Marcus studies two plant cells in biology class. One cell measures $8 \times 10^{-4}$ centimeter across. The other cell measures $2 \times 10^{-3}$ centimeter across. Marcus wants to know how many times greater in size the larger cell is.
He compares the sizes of the cells using these steps:

1. Divide the whole number factors: $8 \div 2=4$
2. Divide the powers of $10: 10^{-3} \div 10^{-4}=10^{1}=10$
3. Multiply the products: $4 \times 10=40$

He concludes that the larger cell is 40 times greater in size than the smaller cell.
Is Marcus's solution process and conclusion correct? Explain.

Jane says that multiplying a decimal by 100 is the same as multiplying the decimal by three factors of 10 . Is Jane correct? Explain your answer.
$\qquad$
$\qquad$
$\qquad$
Complete the equations.
a. $\quad 0.004 \times 100=0.004 \times 10^{2}=$ $\qquad$
b. $\quad 0.4 \times 1,000=0.4 \times$ $\qquad$ $=$ $\qquad$
c. $600 \div 100=600 \div 10^{2}=$ $\qquad$
d. $0.6 \div$ $\qquad$ $=0.6 \div 10^{1}=$ $\qquad$

Yara multiplies and divides a certain number by the same power of 10 . The product she gets is 40,000 and the quotient she gets is 0.000004 . Find Yara's number and the power of 10 she used. Explain your reasoning.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

The number 0.003 written in scientific notation is $3 \times 10^{-3}$. Why is the exponent negative?
$\qquad$
$\qquad$

Is $4.23 \times 10^{-5}$ greater than 1 or less than 1 ? Explain how you know.
$\qquad$
$\qquad$

The total area of Rhode Island is about $1.5 \times 10^{3}$ square miles. The total area of Georgia is about $6 \times 10^{4}$ square miles. The total area of Georgia is about how many times the total area of Rhode Island?

The total area of Ohio is about $4.5 \times 10^{4}$ square miles.
The total area of Ohio is about how many times the total area of Rhode Island?

Which is greater, $9 \times 10^{-2}$ or $3 \times 10^{-4}$ ? How many times greater is the number you chose than the other number? Explain your reasoning.

The total area of Kansas that is covered by water is about $5 \times 10^{2}$ square miles. The total area of Alaska that is covered by water is about $9.5 \times 10^{4}$ square miles. The total water area of Alaska is about how many times the total water area of Kansas?

Show your work.

Solution: $\qquad$
$\qquad$

## 8.EE. 3

1. Kevin moved from a city to a small town. The population of the city is $6 \times 10^{5}$, which is about 15 times as great as the small town. Which expression could represent the approximate population of the small town?

A $4 \times 10^{3}$
B $4 \times 10^{4}$
C $9 \times 10^{5}$
D $9 \times 10^{6}$
2. Ellentown College has approximately $3 \times 10^{3}$ students and Pengrove University has approximately 30,000 students. How many times as much is the number of students at Pengrove University as the number of students at Ellentown College?

A 1
B 10
C 30

D 100
3. Bianca and Nick are both musicians who sell their songs online. During the same year, Bianca sold $8 \times 10^{5}$ downloads of her songs and Nick sold $4 \times 10^{6}$ downloads of his songs. How many times as much is the number of songs that Nick sold than the number of songs that Bianca sold?

A 2
B 5

C 20
D 40
4.

A certain human red blood cell has a diameter of 0.000007 meters. Which expression represents this diameter, in meters, in scientific notation?

A $7 \times 10^{-6}$
B $7 \times 10^{-5}$

C $7 \times 10^{6}$
D $7 \times 10^{5}$

A school club had a T-shirt sale to raise money. After the sale, an inventory showed that 108 blue T-shirts and 96 green T-shirts had been sold. The sizes of these T-shirts included 60 small, 86 medium, and 58 large. Which table correctly represents these data?

NUMBER OF T-SHIRTS SOLD

A | Color | Small | Medium | Large |
| :--- | :---: | :---: | :---: |
| Blue | 60 | 86 | 58 |
| Green | 60 | 86 | 58 |

NUMBER OF T-SHIRTS SOLD

B | Color | Small | Medium | Large |
| :--- | :---: | :---: | :---: |
| Blue | 34 | 46 | 28 |
| Green | 26 | 40 | 30 |

NUMBER OF T-SHIRTS SOLD

C | Color | Small | Medium | Large |
| :--- | :---: | :---: | :---: |
| Blue | 30 | 43 | 29 |
| Green | 30 | 43 | 29 |

NUMBER OF T-SHIRTS SOLD

D | Color | Small | Medium | Large |
| :--- | :---: | :---: | :---: |
| Blue | 26 | 40 | 30 |
| Green | 34 | 46 | 28 |

The owner of a coffee shop compared the amount of hot coffee per day, in fluid ounces, sold and the daily high temperature, in degrees Fahrenheit, per day. Her data are shown in the scatter plot below.


If these data are modeled by the line $y=-5.9 x+850$, which statement best describes a valid prediction the owner could make?

A For each temperature increase of $10^{\circ} \mathrm{F}$, the shop can expect to sell about 60 fluid ounces more hot coffee.

B For each temperature decrease of $10^{\circ} \mathrm{F}$, the shop can expect to sell about 6 fluid ounces more hot coffee.

C On a day with a high temperature of $0^{\circ} \mathrm{F}$, the shop can expect to sell about 145 fluid ounces of hot coffee.

D On a day with a high temperature of $0^{\circ} \mathrm{F}$, the shop can expect to sell about 850 fluid ounces of hot coffee.

Ms. Streffacio
Class: $\qquad$
I can:

## Do Now (3 minutes to complete):

Use the information in the table to solve the problem.

| Orbiting Body | Approximate Distance from the Sun (in miles) |
| :--- | :---: |
| Mercury | $36,300,000$ |
| Mars | $142,000,000$ |
| Neptune | $2,800,000,000$ |
| Pluto | $3,670,000,000$ |

## Show your work.

Write each distance in scientific notation.
Mercury $\qquad$

Mars

Neptune $\qquad$

Pluto
Neptune is about how many times as far from the Sun as Mars is from the Sun?

## Solution:

## Teacher Model (10 minutes) You Watch, Listen, Copy:

The mass of Earth is approximately $5.97 \times 10^{24}$ kilograms. The mass of Venus is approximately $4,870,000,000,000,000,000,000,000$ kilograms. What is the difference between the approximate masses, in kilograms, of Earth and Venus? Express your answer in scientific notation.

Show your work.

## Check for Understanding-Did you understand the Model? (2 minutes) Teacher will check!

Determine the difference in the populations of Texas and North Dakota. In 2012, Texas had a population of about 26 million people, and North Dakota had a population of about $6.9 \times 10^{4}$.

## We Do Together (10 minutes):

Toshi and Owen need to add $4.9 \times 10^{9}$ and $4.1 \times 10^{7}$. Toshi says they must use the expression $\left.490 \times 10^{7}\right)+\left(4.1 \times 10^{7}\right)$. Owen says they must use the expression $\left(4.9 \times 10^{9}\right)+\left(0.041 \times 10^{9}\right)$. Are neither, one, or both students correct? Explain.
$\qquad$
$\qquad$

Final Check for Understanding before I send you to Independent Practice! Teacher will Check (4 minutes):

Paul says that $\left(3.14 \times 10^{5}\right)+\left(2.53 \times 10^{4}\right)=5.67 \times 10^{5}$. Is Paul correct? Explain.

## Independent Practice (In designated groups or on your own):

Evaluate $\frac{\left(7.3 \times 10^{6}\right)+\left(2.4 \times 10^{7}\right)}{\left(4 \times 10^{4}\right)}$.
Show your work.

Answer

In October 2009, there were approximately $5 \times 10^{7}$ members of a website. In January 2013, there were approximately $2 \times 10^{8}$ members. How many more members were there in January 2013 than in October 2009? Write your answer in scientific notation.

There were $\qquad$ more members in January 2013 than in October 2009.

# Stalactites are cone-shaped formations that hang from the ceilings of underground caverns. Stalactites can grow at the rate of about 0.005 inch per year. At this rate, what is the length of a stalactite that grows for $7.5 \times 10^{4}$ years? <br> <br> Show your work. 

 <br> <br> Show your work.}

## Solution

A company spends a total of $\$ 64,500,000$ on salaries for its workers. If the company has $1.5 \times 10^{3}$ workers, what is the average salary per worker?

Show your work.

## Solution

Why is it unnecessary to make the exponents the same before multiplying numbers expressed in scientific notation?

Use the information in the table to solve the problem.

| Country | Estimated Population |
| :--- | ---: |
| China | $1,390,000,000$ |
| Germany | $82,700,000$ |
| Martinique | 405,000 |

Write each population in scientific notation.
China $\qquad$
Germany $\qquad$
Martinique $\qquad$
The population of Germany is about how many times the population of Martinique? Explain your reasoning.
$\qquad$
$\qquad$

A scientist uses $2.8 \times 10^{12}$ cells in one experiment, which is 2,000 times the number of cells she uses in a second experiment. Write the number of cells the scientist used in her second experiment in scientific notation. Explain your answer.
$\qquad$
$\qquad$
$\qquad$

Find the perimeter of the rectangle in scientific notation.
$2.4 \times 10^{3} \mathrm{~cm}$
Show your work.

## The area of the Southern Ocean is about $7.85 \times 10^{6}$

 square miles. The difference between the areas of the Indian Ocean and the Southern Ocean is about $1.865 \times 10^{7}$ square miles. Explain how to find the area of the Indian Ocean. Then find the area.$\qquad$
$\qquad$
$\qquad$
$\qquad$

Is the value of $\left(1.7 \times 10^{4}\right) \times\left(2.1 \times 10^{-8}\right)$ greater than 1 or between 0 and 1 ? Explain your reasoning.

The thickness of a U.S. penny is $5.98 \times 10^{-2}$ inch.
What is the height of a stack of $2.5 \times 10^{4}$ pennies?

## Show your work.

## Solution:

$\qquad$

The speed of light is about $1.86 \times 10^{5}$ miles per second.
How many miles will light travel in 4,200,000 seconds?
$\qquad$
Find the area of the rectangle in scientific notation. $\quad \square .4 \times 10^{5} \mathrm{~mm}$

A container at a paper clip factory holds $2.1 \times 10^{3}$ pounds of paper clips. There are $9.6 \times 10^{5}$ paper clips in the container. Find the approximate weight of each paper clip in ounces. (1 pound = 16 ounces)

## Show your work.

A glass marble factory produces $4.5 \times 10^{4}$ marbles in 1,800 minutes. What is the factory's unit rate of production in marbles per minute? Write the answer in scientific notation.

## Show your work.

Which operation do you need to use to solve this problem?

Solution: $\qquad$

Evaluate: $\frac{\left(5.6 \times 10^{6}\right)-340,000}{2 \times 10^{3}}$

## Show your work.

A computer performs a calculation in $2.5 \times 10^{-5}$ seconds to solve a math problem. How long does the computer need to calculate the solutions to $3 \times 10^{6}$ math problems?

Write your answer in standard form.
Show your work.

Answer: __ seconds

Consider the expression $\frac{\left(6.2 \times 10^{17}\right)+\left(1.2 \times 10^{15}\right)}{\left(4 \times 10^{-6}\right)}$.
Part A
Evaluate the expression. Write your answer in scientific notation.
Show your work.

Answer:

## Part B

Describe two different ways to use the properties of exponents to rewrite the numerator of the expression.

